

# Charged LFV, RGEs and algebraic renormalization

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- LFV, charged LFV
- RGEs
- Algebraic renormalization

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# Motivation for CLFV

- SM does not allow LFV and predicts massless neutrinos
- neutrino oscillations :  $m_\nu \neq 0$ , LFV exists: sign for a physics BSM

$$\sin^2 \theta_{12} = 0.307 \pm 0.013$$

$$\sin^2 \theta_{23} = 0.51 \pm 0.04 \quad \text{normal hierarchy}$$

$$\sin^2 \theta_{23} = 0.50 \pm 0.04 \quad \text{inverted hierarchy}$$

$$\sin^2 \theta_{13} = (2.10 \pm 0.11) \times 10^{-2}$$

$$\Delta m_{12}^2 = (7.53 \pm 0.18) \times 10^{-5} \text{eV}^2 \quad \text{normal hierarchy}$$

$$\Delta m_{23}^2 = (2.45 \pm 0.05) \times 10^{-3} \text{eV}^2 \quad \text{inverted hierarchy}$$

- scale of new physics not determined by neutrino oscillations
- CLFV,  $d_e > 10^{-33}$  e cm,  $(a_\mu^{th} - a_\mu^{exp})/a_\mu^{exp} > (a_\mu \text{ sensitivity})$ : would be independent sign for a physics BSM
- information on a scale of new physics

# Experiment

Observable	Upper Limit	Future sensitivity
$B(\mu \rightarrow e\gamma)$	$2.4 \times 10^{-12}$ [1]	$1 - 2 \times 10^{-13}$ [6], $10^{-14}$ [6]
$B(\mu \rightarrow eee)$	$10^{-12}$ [2]	$10^{-16}$ [8], $10^{-17}$ [7]
$R_{\mu e}^{\text{Ti}}$	$4.3 \times 10^{-12}$ [3],	$3 - 7 \times 10^{-17}$ [10, 9], $10^{-18}$ [11, 7]
$R_{\mu e}^{\text{Au}}$	$7 \times 10^{-13}$ [4]	$3 - 7 \times 10^{-17}$ [10, 9], $10^{-18}$ [11, 7]
$B(\tau \rightarrow e\gamma)$	$3.3 \times 10^{-8}$ [5]	$1 - 2 \times 10^{-9}$ [13, 12]
$B(\tau \rightarrow \mu\gamma)$	$4.4 \times 10^{-8}$ [5]	$2 \times 10^{-9}$ [13, 12]
$B(\tau \rightarrow eee)$	$2.7 \times 10^{-8}$ [5]	$2 \times 10^{-10}$ [13, 12]
$B(\tau \rightarrow e\mu\mu)$	$2.7 \times 10^{-8}$ [5]	$10^{-10}$ [12]
$B(\tau \rightarrow \mu\mu\mu)$	$2.1 \times 10^{-8}$ [5]	$2 \times 10^{-10}$ [13, 12]
$B(\tau \rightarrow \mu ee)$	$1.8 \times 10^{-8}$ [5]	$10^{-10}$ [12]
$d_e$	$0.87 \times 10^{-28}$ ecm [1]	$10^{-29} - 10^{-31}$ ecm [14]
$a_{\mu}^{\text{exp}}$	Sensitivity ( $\delta a_{\mu}/a_{\mu}$ )	Future sensitivity
$(116592089) \times 10^{-11}$	$0.54 \times 10^{-6}$ [14]	$0.14 \times 10^{-6}$ [15, 16]

Table 1: Current upper limits and future sensitivities of CLFV observables, electron EDM and muon MDM.

- [1] PDG, Chin. Phys. C 40 (2016) 100001
- [2] U. Bellgardt, (SINDRUM) NPB 299 (1988) 1
- [3] C. Dohmen, (SINDRUM II) PLB 317 (1993) 631
- [4] W. Bertl, EPJ C47 (2006) 337
- [5] See A.I., arXiv:1212.5939, Ref. [11]
- [6] B.A. Golden (MEG) PhD 2012, J. Adam (MEG) PhD 2012
- [7] J.L. Hewett, arXiv:1205.2671
- [8] N. Berger, ( $\mu 3e$ ) JPCS 408, 122070 (2013)
- [9] A. Kurup (COMET) NPPS 218, 38 (2011)
- [10] R.J. Abrams ( $\text{Mu}2e$ ) arXiv:1211.7019; E.C. Dukes NPPS 218 (2011) 44
- [11] Y. Kuno (PRISM) NPPS 149 (2005) 376; R.J. Barow (PRISM) , NPPS 218 (2011) 44
- [12] K. Hayasaka, JPCS 171 (2009) 012079
- [13] M. Bona (SuperB), arXiv:0709.0451
- [14] M. Jung, JHEP 1305 (2013) 168
- [15] B.L. Roberts NPPS 218 (2011) 237
- [16] G. Venanzoni, arXiv:1203.1501; J.Phys.Conf.Ser. 349 (2012) 012008

# Used Models

## Non-SUSY models CSS ISS

SS=see-saw, M=constrained, I=inverse

$$\mathcal{L}_{CSS} = \mathcal{L}_{SM} - (\overline{\nu_R} Y_\nu \tilde{H} l + \frac{1}{2} \overline{\nu_R^c} M \nu_R + h.c.)$$

$$\mathcal{L}_{ISS} = \mathcal{L}_{SM} - (\overline{\nu_R} Y_\nu \tilde{H} l + \overline{\nu_R} M_\nu x_L + \frac{1}{2} \overline{x_L^c} M x_L + h.c.)$$

## SUSY models: superpotential

$$W_{CSS} = W_{MSSM} + Y_\nu^{ij} N_{iR}^c H_u \cdot L_{jL} + \frac{1}{2} M_M^{ij} N_{iR}^c N_{jR}^c$$

$$W_{ISS} = W_{MSSM} + Y_\nu^{ij} \overline{N}_i^c H_u \cdot L + (M_\nu)^{ij} \overline{N}_i^c X_{jL} + \frac{1}{2} \mu^{ij} X_{iL}^c X_{jL}$$

## LFV induced by neutrino terms

- Borzumati, Masiero PRL (1986) 961 : MSSM+3 $\nu_R$  with SS-I has only LFV induced by soft SUSY breaking terms and  $s_L \sim \sqrt{m_\nu/M_M}$
- models defined by  $W_{CSS}$  and  $W_{ISS}$  have additional neutrino induced LFV

# LFV in low-scale seesaw models ( $\nu_R$ MSSM)

- Neutrino induced LFV mechanism:  $m_N \gtrsim 1$  TeV

- Neutrino mass matrix ( $m_e$  diagonal basis; at scale  $m_N$ )

$$(M_\nu)_{CSS} = \begin{pmatrix} 0 & m_D^T \\ m_D & M_M \end{pmatrix}, \quad M_\nu B^{\nu L \dagger} = 0, \quad m_{n_i} \approx m_{n_j}, \quad i, j > 3, \\ m_D = \sqrt{2} M_W s_\beta g^{-1} Y_\nu^\dagger$$

$$(M_\nu)_{ISS} = \begin{pmatrix} 0 & m_D^T & 0 \\ m_D & 0 & M_R \\ 0 & M_R^T & \mu_X \end{pmatrix}, \quad m_D = \sqrt{2} M_W s_\beta g^{-1} Y_\nu^\dagger$$

CSS : LFV induced by  $B^{\nu R} = v_u Y_\nu / (\sqrt{2} M_M)$ ,

- $\nu_\ell^{SM} = (Bn)_\ell = (B^{\nu L} \nu_L)_\ell + (B^{\nu R} \nu_R)_\ell$  :  $B$  diagonalizes  $M_\nu$
- $\nu$  masses : **sym. breaking** ( $m_{n_i} \neq m_{n_j}$ ,  $M_\nu B^\nu \neq 0$ ) and radiatively induced

ISS : LFV induced by  $B^{\nu R}$ ,  $B^{xL}$

- $\nu_\ell^{SM} = (Bn)_\ell = (B^{\nu L} \nu_L)_\ell + (B^{\nu R} \nu_R)_\ell + (B^{xL} x_L)_\ell$  :  $B$  diagonalizes  $M_\nu$
- $\nu$  masses :  $m_\nu = m_D^T M_R^{T-1} \mu_X M_R^{-1} m_D$

- Sneutrino mass matrix (CSS MSSM)

$$M_{\tilde{\nu}}^2 = \begin{pmatrix} H_1 & N & 0 & M \\ N^\dagger & H_2^T & M^T & M_B \\ 0 & M^* & H_1^T & N^* \\ M^\dagger & M_B^\dagger & N^T & H_2 \end{pmatrix}, \quad M_{\tilde{\nu}}^2 \xrightarrow{SUSY} \begin{pmatrix} M_\nu M_\nu^\dagger & 0_{6 \times 6} \\ 0_{6 \times 6} & M_\nu^\dagger M_\nu \end{pmatrix}$$

$$H_1 = m_{\tilde{L}}^2 + \left(\frac{1}{2} M_Z^2 c_{2\beta} \mathbf{1}\right) + (m_D m_D^\dagger)$$

$$H_2 = m_{\tilde{\nu}}^2 + (m_D^\dagger m_D) + (M_M^\dagger M_M)$$

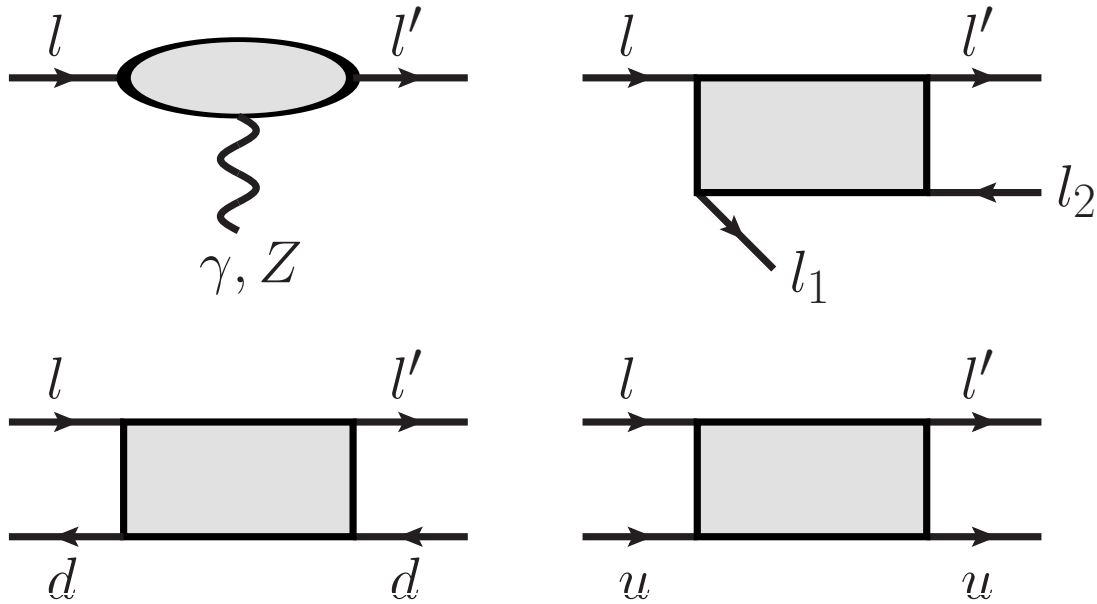
$$M = m_D (A_\nu - \mu c t_\beta)$$

$$N = m_D M_M^\dagger, \quad M_B \equiv \frac{1}{2} B_{IJ} (M_\nu)_{IJ} \rightarrow 0; b_\nu$$

-  $N$ - $\tilde{N}$  sector nearly supersymmetric if  $m_N > m_{SUSY}$  and  $Y_\nu \leq 0.2$

# Amplitudes

## Amplitudes : diagrams



We took  $\tan \beta < 20$ . Neutral Higgs ( $h, H, A$ ) contr. not taken into account



## Amplitudes : structure

$$\mathcal{T}_\mu^{\gamma l' l} = \frac{e \alpha_w}{8\pi M_W^2} \bar{l}' [ \underline{(F_\gamma^L)_{l'l} (q^2 \gamma_\mu - \not{q} q_\mu) P_L} + (F_\gamma^R)_{l'l} (q^2 \gamma_\mu - \not{q} q_\mu) P_R ] l, \\ + \underline{(G_\gamma^L)_{l'l} i \sigma_{\mu\nu} q^\nu P_L} + \underline{(G_\gamma^R)_{l'l} i \sigma_{\mu\nu} q^\nu P_R} ] l,$$

$$\mathcal{T}_\mu^{Z l' l} = \frac{g_w \alpha_w}{8\pi \cos \theta_w} \bar{l}' [ \underline{(F_Z^L)_{l'l} \gamma_\mu P_L} + (F_Z^R)_{l'l} \gamma_\mu P_R ] l,$$

$$\mathcal{T}_\gamma^{l'l_1 l_2} = \frac{\alpha_w^2 s_w^2}{2M_W^2} \{ \delta_{l_1 l_2} \bar{l}' [ \underline{(F_\gamma^L)_{l'l} \gamma_\mu P_L} + (F_\gamma^R)_{l'l} \gamma_\mu P_R ] l \bar{l}_1 \gamma^\mu l_2^C - [l' \leftrightarrow l_1] \}, \\ + \frac{(\not{p} - \not{p}')}{(p - p')^2} ( \underline{(G_\gamma^L)_{l'l} \gamma_\mu P_L} + \underline{(G_\gamma^R)_{l'l} \gamma_\mu P_R} ) l \bar{l}_1 \gamma^\mu l_2^C - [l' \leftrightarrow l_1] \},$$

$$\mathcal{T}_Z^{l'l_1 l_2} = \frac{\alpha_w^2}{2M_W^2} [ \delta_{l_1 l_2} \bar{l}' ( \underline{(F_Z^L)_{l'l} \gamma_\mu P_L} + (F_Z^R)_{l'l} \gamma_\mu P_R ) l \\ \times \bar{l}_1 (g_L^l \gamma^\mu P_L + g_R^l \gamma^\mu P_R) l_2^C - (l' \leftrightarrow l_1) ],$$

$$\begin{aligned}
\mathcal{T}_{\text{box}}^{ll'l_1l_2} &= -\frac{\alpha_w^2}{4M_W^2} \left( \underline{B_{\ell V}^{LL}} \bar{l}' \gamma_\mu P_L l \bar{l}_1 \gamma^\mu P_L l_2^C + \underline{B_{\ell V}^{RR}} \bar{l}' \gamma_\mu P_R l \bar{l}_1 \gamma^\mu P_R l_2^C \right. \\
&\quad + \underline{B_{\ell V}^{LR}} \bar{l}' \gamma_\mu P_L l \bar{l}_1 \gamma^\mu P_R l_2^C + \underline{B_{\ell V}^{RL}} \bar{l}' \gamma_\mu P_R l \bar{l}_1 \gamma^\mu P_L l_2^C \\
&\quad + \underline{B_{\ell S}^{LL}} \bar{l}' P_L l \bar{l}_1 P_L l_2^C + \underline{B_{\ell S}^{RR}} \bar{l}' P_R l \bar{l}_1 P_R l_2^C \\
&\quad + \underline{B_{\ell S}^{LR}} \bar{l}' P_L l \bar{l}_1 P_R l_2^C + \underline{B_{\ell S}^{RL}} \bar{l}' P_R l \bar{l}_1 P_L l_2^C \\
&\quad \left. + \underline{B_{\ell T}^{LL}} \bar{l}' \sigma_{\mu\nu} P_L l \bar{l}_1 \sigma^{\mu\nu} P_L l_2^C + \underline{B_{\ell T}^{RR}} \bar{l}' \sigma_{\mu\nu} P_R l \bar{l}_1 \sigma^{\mu\nu} P_R l_2^C \right) \\
&\equiv -\frac{\alpha_w^2}{4M_W^2} \sum_{X,Y=L,R} \sum_{A=V,S,T} B_{\ell A}^{XY} \bar{l}' \Gamma_A^X l \bar{l}_1 \Gamma_A^Y l_2^C ,
\end{aligned}$$

$\mathcal{T}_{\text{box}}^{ll'dd}$  and  $\mathcal{T}_{\text{box}}^{ll'uu}$  have the same structure as  $\mathcal{T}_{\text{box}}^{ll'l_1l_2}$

- form factors
- new form factors
- the underlined terms contribute to non-SUSY models

## Form factors

### Contributions

1.  $\gamma$ ,  $Z$ , l-box, sl-box;  $h$ ,  $H$ ,  $A$  not included
2. Each form factor in principle has heavy neutrino ( $N$ ), sneutrino ( $\tilde{N}$ ) and soft SUSY breaking  $SB$  contributions, for instance

$$(F_\gamma^L)_{\nu l} = F_{\nu l \gamma}^N + F_{\nu l \gamma}^{L, \tilde{N}} + F_{\nu l \gamma}^{L, SB}$$

A.I., A. Pilaftsis, PRD80 (2009) 091902 :  $N$ ,  $\tilde{N}$ ;  $\gamma$ ,  $Z$ , l-box, sl-box;  $\nu_R MSSM$  (CSS)

M. Hirsch, F. Staub, A. Vicente, Phys.Rev. D85 (2012) 113013, A. Abada, D. Das, A. Vicente, C. Weiland:  $N$ ,  $\tilde{N}$ , SB;  $\gamma$ ,  $Z$ , higgs, l-box, sl-box, but no  $N$ -box, MSISM (ISS)

A.I., A. Pilaftsis, L. Popov, PRD 87 (2013) 5, 053014:  $N$ ,  $\tilde{N}$ , SB;  $\gamma$ ,  $Z$ , l-box, sl-box but no higgs;  $\nu_R MSSM$

M. E. Krauss, W. Porod, F. Staub, A. Abada, A. Vicente, C. Weiland, Phys.Rev. D90 (2014), 013008, MSISM:  $Z$  not dominant

A. Abada, Manuel E. Krauss, W. Porod, F. Staub, A. Vicente, C. Weiland JHEP 1411 (2014) 048: all contributions, detailed analysis

# Dipole moments

## Lagrangian and dipole moments

$$\mathcal{L} = \bar{l}[\gamma(i\partial^\mu + eA^\mu) - m_l - \frac{e}{2m_l}\sigma^{\mu\nu}(F_l + iG_l\gamma_5)\partial_\nu A_\mu]l$$

$$a_l = F_l \quad d_l = eG_l/m_l$$

## Amplitude and dipole moments

$$i\mathcal{T}^{\gamma ll} = \frac{ie\alpha_w}{8\pi M_W^2}[(G_\gamma^L)_{ll}i\sigma_{\mu\nu}q^\nu P_L + (G_\gamma^R)_{ll}i\sigma_{\mu\nu}q^\nu P_R]$$

$$a_l = \frac{\alpha_w m_l}{8\pi M_W^2}[(G_\gamma^L)_{ll} + (G_\gamma^R)_{ll}] \quad d_l = \frac{e\alpha_w}{8\pi M_W^2}i[(G_\gamma^L)_{ll} - (G_\gamma^R)_{ll}]$$

## Possible sources of lepton EDM (CPV)

$$A_\nu = h_\nu A_0 e^{i\phi} \quad -(A_\nu)^{ij} \tilde{\nu}_R^c (h_{uL}^+ \tilde{e}_{jL} - h_{uL}^0 \tilde{\nu}_{jL})$$

$$b_\nu = B_0 e^{i\theta} m_N \mathbf{1}_3 \quad (b_\nu)_{ii} \tilde{\nu}_{Ri} \tilde{\nu}_{Ri}$$

$$\Delta_{\text{CP}}^{LR} = \tilde{B}_{lkA}^L \tilde{B}_{lkA}^{R*} \quad \Delta_{\text{CP}}^{RL} = \tilde{B}_{lkA}^R B_{lkA}^{L*}$$

## Scaling behaviour of MSSM contribution dipole moments

$$a_l^{MSSM} \propto \frac{m_l^2}{M_{SUSY}^2} \tan \beta \operatorname{sign}(\mu M_{1,2}) \quad (\text{checked})$$

$$d_l \propto \frac{e m_l}{M_{SUSY}^2} \tan \beta \sin(\phi_{CP}) \quad (\text{expected, checked})$$

$$d_l \propto \frac{e m_l f(m_0)}{M_N^x} \tan \beta, \quad 2/3 < x < 1 \quad (\text{found})$$

A. Pilaftsis, L. Popov, AI, PRD 89 (2014) no.1, 015001 : 1-loop CSS MSSM

A. Abada, T. Toma, JHEP 02 (2016) 174, JHEP 08 (2016) 079 : 2 loop ISS MSSM

# mSUGRA Framework

## Boundary conditions and RGEs:

1. SM parameters at  $M_Z$  scale (Fusaoka and Koide PRD57 (1998) 3986).
2. Neutrino Yukawa and heavy neutrino masses at heavy neutrino scale  $m_N$ ,  
(Pilaftsis PRL95 (081602) 2005, PRD72 (2005) 113001, PRD83 (2011) 076007: U(1) fl. sym.;  
J. Kersten, A.Y. Smirnov, PRD76 (2007) 073005):  $A_4$  fl. sym.)

$$m_{N_i} = m_N,$$

$$Y_\nu = \begin{pmatrix} 0 & 0 & 0 \\ ae^{-\frac{i\pi}{4}} & be^{-\frac{i\pi}{4}} & ce^{-\frac{i\pi}{4}} \\ ae^{\frac{i\pi}{4}} & be^{\frac{i\pi}{4}} & ce^{\frac{i\pi}{4}} \end{pmatrix} \quad Y_\nu = \begin{pmatrix} a^* & b^* & c^* \\ a^* e^{-\frac{2\pi i}{3}} & b^* e^{-\frac{2\pi i}{3}} & c^* e^{-\frac{2\pi i}{3}} \\ a^* e^{\frac{2\pi i}{3}} & b^* e^{\frac{2\pi i}{3}} & c^* e^{\frac{2\pi i}{3}} \end{pmatrix}$$

3. mSUGRA conditions at gauge unification scale  $g_1 = g_2 = g_3$ ,

$$\begin{aligned} m_{H_1, H_2}^2 &= m_0^2, & m_{\tilde{u}, \tilde{d}, \tilde{e}, \tilde{n}}^2 &= m_0^2 \mathbf{1} \\ M_{1,2,3} &= M_0, & A_{u,d,e,n} &= A_0 Y_{u,d,e,n}. \end{aligned}$$

4. MSSM+3N RGE equations (P. Chankowski and S. Pokorski, IJMP A17 (2002) 575,  
S. Petcov et al. NPB676 (2004) 453).

# Physical observables studied in considered models

$\mu^- \rightarrow e^- \gamma$	$\tau^- \rightarrow e^- \eta$	$\tau^- \rightarrow e^- \pi^0 \pi^0$	$K^+ \rightarrow \pi^+ e^\mp \mu^\pm$
$\mu^- \rightarrow e^- e^+ e^-$	$\tau^- \rightarrow \mu^- \eta$	$\tau^- \rightarrow \mu^- \pi^0 \pi^0$	$\bar{B}^0 \rightarrow e^\mp \mu^\pm$
$\tau^- \rightarrow e^- e^+ e^-$	$\tau^- \rightarrow e^- \rho^0$	$\tau^- \rightarrow e^- \eta \eta$	$\bar{B}^0 \rightarrow e^\mp \tau^\pm$
$\tau^- \rightarrow \mu^- \mu^+ \mu^-$	$\tau^- \rightarrow \mu^- \rho^0$	$\tau^- \rightarrow \mu^- \eta \eta$	$\bar{B}^0 \rightarrow \mu^\mp \tau^\pm$
$\tau^- \rightarrow e^- \mu^+ \mu^-$	$\tau^- \rightarrow e^- \phi$	$\tau^- \rightarrow e^- \pi^0 \eta$	$\bar{B}_s^0 \rightarrow e^\mp \mu^\pm$
$\tau^- \rightarrow \mu^- e^+ e^-$	$\tau^- \rightarrow \mu^- \phi$	$\tau^- \rightarrow \mu^- \pi^0 \eta$	$\bar{B}_s^0 \rightarrow e^\mp \tau^\pm$
$\tau^- \rightarrow e^+ \mu^- \mu^-$	$\tau^- \rightarrow e^- K^0$	$\tau^- \rightarrow e^- K^0 \bar{K}^0$	$\bar{B}_s^0 \rightarrow \mu^\mp \tau^\pm$
$\tau^- \rightarrow \mu^+ e^- e^-$	$\tau^- \rightarrow \mu^- K^0$	$\tau^- \rightarrow \mu^- K^0 \bar{K}^0$	$\bar{B}^- \rightarrow \pi^- e^\mp \mu^\pm$
$\mu^- Ti \rightarrow e^- Ti$	$\tau^- \rightarrow e^- K^{*0}$	$\pi^0 \rightarrow e^- \mu^+$	$\bar{B}^- \rightarrow \pi^- e^\mp \tau^\pm$
$\mu^- Au \rightarrow e^- Au$	$\tau^- \rightarrow \mu^- K^{*0}$	$\eta \rightarrow e^- \mu^+$	$\bar{B}^- \rightarrow \pi^- \mu^\mp \tau^\pm$
$Z \rightarrow e^- \mu^+$	$\tau^- \rightarrow e^- \bar{K}^{*0}$	$K_L \rightarrow e^- \mu^+$	$\bar{B}^0 \rightarrow \bar{K}^0 e^\mp \mu^\pm$
$Z \rightarrow e^- \tau^+$	$\tau^- \rightarrow \mu^- \bar{K}^{*0}$	$K_L \rightarrow \pi^0 e^- \mu^+$	$\bar{B}^0 \rightarrow \bar{K}^0 e^\mp \tau^\pm$
$Z \rightarrow \mu^- \tau^+$	$\tau^- \rightarrow e^- \pi^+ \pi^-$	$\pi^0 \rightarrow e^- \mu^+$	$\bar{B}^0 \rightarrow \bar{K}^0 \mu^\mp \tau^\pm$
	$\tau^- \rightarrow \mu^- \pi^+ \pi^-$	$\eta \rightarrow e^- \mu^+$	$\bar{B}_s^0 \rightarrow \eta e^\mp \mu^\pm$
$\tau^- \rightarrow e^- \pi^0$	$\tau^- \rightarrow e^- K^+ K^-$	$K_L \rightarrow e^\mp \mu^\pm$	$\bar{B}_s^0 \rightarrow \eta e^\mp \tau^\pm$
$\tau^- \rightarrow \mu^- \pi^0$	$\tau^- \rightarrow \mu^- K^+ K^-$	$K_L \rightarrow \pi^0 e^\mp \mu^\pm$	$\bar{B}_s^0 \rightarrow \eta \mu^\mp \tau^\pm$

$$\begin{aligned}
\bar{B}_s^0 &\rightarrow \eta' e^\mp \mu^\pm \\
\bar{B}_s^0 &\rightarrow \eta' e^\mp \tau^\pm \\
\bar{B}_s^0 &\rightarrow \eta' \mu^\mp \tau^\pm \\
B^- &\rightarrow K^{*-} e^\mp \mu^\pm \\
B^- &\rightarrow K^{*-} e^\mp \tau^\pm \\
B^- &\rightarrow K^{*-} \mu^\mp \tau^\pm \\
\bar{B}^0 &\rightarrow K^{*0} e^\mp \mu^\pm \\
\bar{B}^0 &\rightarrow K^{*0} e^\mp \tau^\pm \\
\bar{B}^0 &\rightarrow K^{*0} \mu^\mp \tau^\pm \\
\bar{B}_s^0 &\rightarrow \phi e^\mp \mu^\pm \\
\bar{B}_s^0 &\rightarrow \phi e^\mp \tau^\pm \\
\bar{B}_s^0 &\rightarrow \phi \mu^\mp \tau^\pm
\end{aligned}$$



# Solved problems, Work in progress, Questions

1. 1 loop RGEs – solved – Marija Mađor Božinović
2. Algebraic renormalization (AR) – in progress – Jiangyang You
3. Implementation of AR techniques in evaluation of 2-loop RGEs and amplitudes  
– (many) questions – topic for a talk during next visit to Dresden

# Thank you

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# BACKUP SLIDES

**LFV** : Borzumati, Masiero PRL (1986) 961

$$\mathcal{M}_{\tilde{e}}^2 = \begin{pmatrix} M_{\tilde{L}}^2 + (m_e m_e^\dagger) + D_1 \mathbf{1} & m_e (A_e^* - \mu t_\beta \mathbf{1}) \\ (A_e^T - \mu^* t_\beta \mathbf{1}) m_e^\dagger & M_{\tilde{e}}^2 + (m_e^\dagger m_e) + D_2 \mathbf{1} \end{pmatrix}$$

$$(\Delta M_{\tilde{L}}^2)_{ij} \approx -\frac{1}{8\pi^2} (3m_0^2 + A_0^2) h_\nu^\dagger h_\nu \log \frac{M_X}{M_N},$$

$$(A_e)_{ij} \approx -\frac{3}{8\pi^2} A_0 h_e h_\nu^\dagger h_\nu \log \frac{M_X}{M_N},$$

**Since recently** : in SUSY LFV studies LFV induced by soft-SUSY breaking terms only

# LFV in low-scale seesaw models ( $\nu_R$ MSSM)

- New supersymmetric LFV mechanism:  $m_N \gtrsim 1$  TeV

- LFV parameters in  $N$  sector:

$$\Omega_{\ell\ell'} = \frac{v_u^2}{2m_N^2} (h_\nu^\dagger h_\nu)_{\ell\ell'} = B_{\ell N_i}^* B_{\ell' N_i}$$

- Neutrino mass matrix ( $m_e$  diagonal basis; at scale  $m_N$ )

$$M_\nu = \begin{pmatrix} 0 & m_D^T \\ m_D & M_M \end{pmatrix}, \quad M_\nu B^{\nu\dagger} = 0, \quad m_{n_i} \approx m_{n_j}, \quad i, j > 3,$$

$$m_D = \sqrt{2} M_W s_\beta g^{-1} h_\nu^\dagger$$

$$h_\nu = \begin{pmatrix} 0 & 0 & 0 \\ ae^{-i\pi/4} & be^{-i\pi/4} & ce^{-i\pi/4} \\ ae^{i\pi/4} & be^{i\pi/4} & ce^{i\pi/4} \end{pmatrix} \quad h_\nu = \begin{pmatrix} a^* & b^* & c^* \\ a^* e^{-2\pi i/3} & b^* e^{-2\pi i/3} & c^* e^{-2\pi i/3} \\ a^* e^{2\pi i/3} & b^* e^{2\pi i/3} & c^* e^{2\pi i/3} \end{pmatrix}$$

•  $\nu_\ell^{SM} = (Bn)_\ell = (B^\nu \nu)_\ell + (B^N N)_\ell$  :  $B$  diagonalizes  $M_\nu$

•  $\nu$  masses : sym. breaking; radiatively induced

# Explanation of form factor structure in non-SUSY models

- The dominant terms of vertices appear in combinations that assure the  $\gamma_\mu P_L$  structure in the  $l \rightarrow l' \gamma$  and  $l \rightarrow l' Z$  effective vertices.
- The box diagrams : Dirac (LNC currents) type diagrams have automatically  $\gamma_\mu P_L \times \gamma^\mu P_L$  structure. Majorana (LNV currents) type diagrams have  $\gamma_\mu P_L \times \gamma^\mu P_L$  structure only after Fiertz transformations, which replace the LNV currents by LNC currents.

In SUSY models the structure of amplitudes is more complex than in non-SUSY models. The vertices of the SUSY models and Fiertz transformations, necessary to receive the appropriate currents, lead to the most general structure of the amplitudes permitted by the Dirac algebra.

# SUSY limit; cancelations

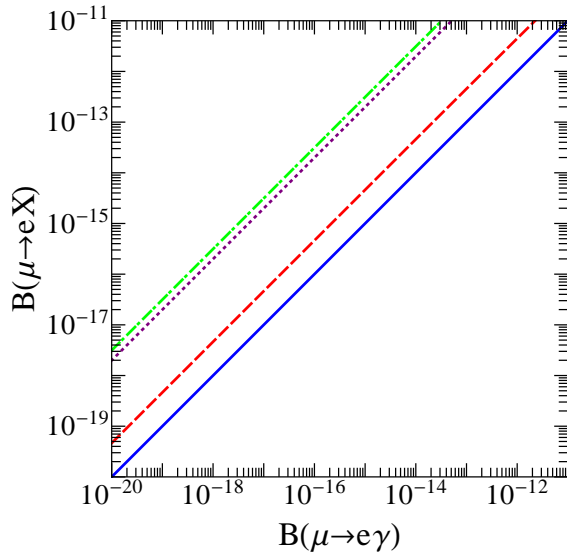
-  $\tilde{m}_{\tilde{\chi}_{1,2}}^2 \xrightarrow{SL} M_W^2, \quad t_\beta \xrightarrow{SL} 1, \quad \mu \xrightarrow{SL} 0$  (Barbieri, Giudice PLB309)

-  $(G_\gamma^{ll'})^N + (G_\gamma^{ll'})^{\tilde{N}} \stackrel{SL}{=} 0:$  Ferrara, Remiddi PLB53 (1974) 347

# Numerical results for CLFV

## Choice of parameters

1.  $m_0 = 1000$  GeV,  $A_0 = -3000$  GeV,  $M_{1/2} = 1000$  GeV  
consistent with  $m_h \approx 126$  GeV  
consistent with  $m_{\tilde{g}}, m_{\tilde{q}} > 1$  GeV  
in agreement with lightest neutralino as a dark matter candidate
2.  $sign(\mu) > 0$
3.  $\tan \beta = 10$  in most of calculations
4. Yukawa parameters:  
model 1:  $a = b, c = 0; a = c, b = 0; b = c, a = 0$   
model 2:  $a = b = c$   
Perturbativity condition  $Tr h_\nu^\dagger h_\nu < 4\pi$ :  
model 1:  $a < 0.34$   
model 2:  $a < 0.23$
5.  $m_N < 10$  TeV: consistency with resonant leptogenesis



$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

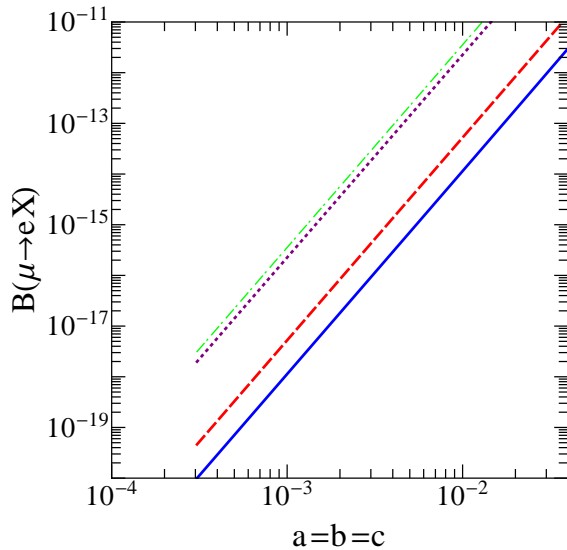
$$m_N = 1 \text{ TeV}, \tan \beta = 10$$

$$\text{model 2: } a = b = c$$

$$\text{perturbativity condition } Tr h_\nu^\dagger h_\nu < 4\pi$$

quadratic Yukawa dependence

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti}, B(\mu \rightarrow eee) > B(\mu \rightarrow e\gamma)$$



$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

$$m_N = 1 \text{ TeV}, \tan \beta = 10$$

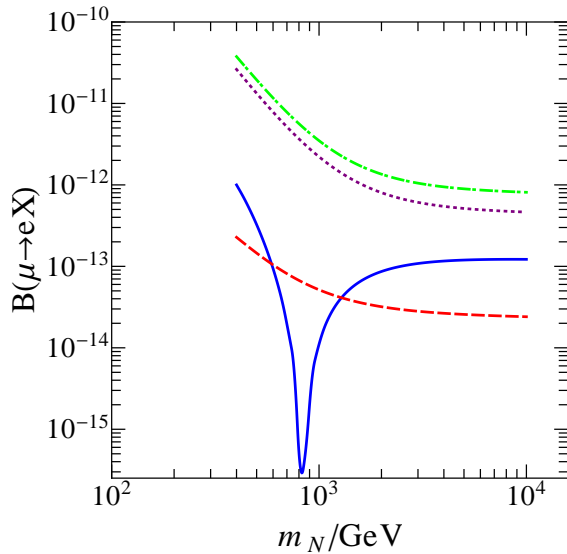
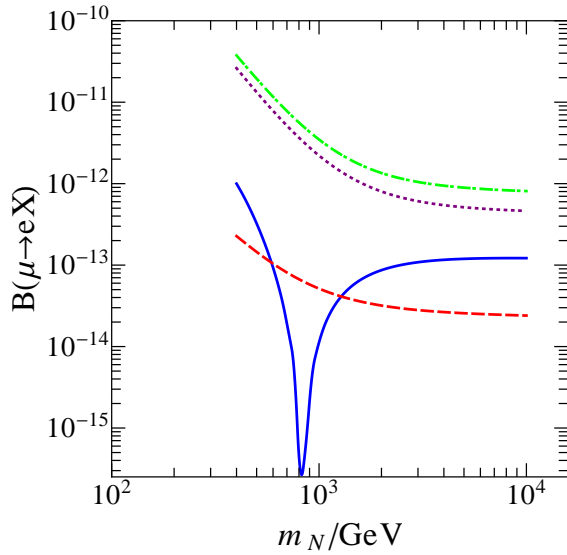
$$\text{model 2: } a = b = c$$

$$\text{perturbativity condition } Tr h_\nu^\dagger h_\nu < 4\pi$$

quadratic Yukawa dependence

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti}, B(\mu \rightarrow eee) > B(\mu \rightarrow e\gamma)$$





$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

$$a: B(\mu \rightarrow eee) = 10^{-12} \text{ for } m_N = 400 \text{ GeV}$$

$$\tan \beta = 10$$

$$\text{model 2: } a = b = c$$

$B(\mu \rightarrow e\gamma)$ : cancelation of  $N$ ,  $\tilde{N}$  and  $SB$  contributions

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti} > B(\mu \rightarrow e\gamma)$$

$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

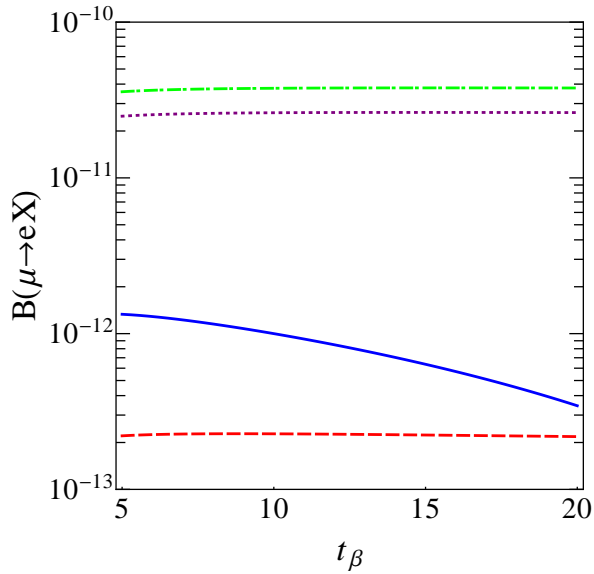
$$a: B(\mu \rightarrow eee) = 10^{-12} \text{ for } m_N = 400 \text{ GeV}$$

$$\tan \beta = 10$$

$$\text{model 1: } a = b, c = 0$$

$B(\mu \rightarrow e\gamma)$ : cancelation of  $N$ ,  $\tilde{N}$  and  $SB$  contributions

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti} > B(\mu \rightarrow e\gamma)$$



$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

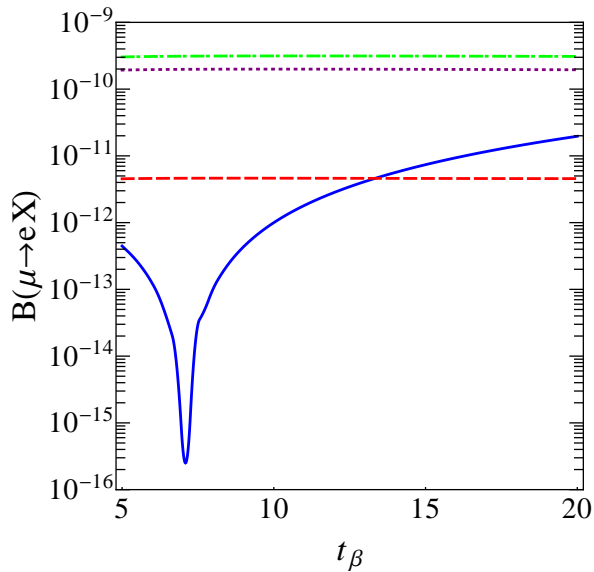
$$m_N = 400 \text{ GeV}$$

$$a: B(\mu \rightarrow eee) = 10^{-12} \text{ for } \tan \beta = 10$$

$$\text{model 2: } a = b = c$$

weak dependence on  $\tan \beta$

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti} > B(\mu \rightarrow e\gamma)$$



$$B(\mu \rightarrow e\gamma) \quad B(\mu \rightarrow eee) \quad R_{\mu e}^{Ti} \quad R_{\mu e}^{Au}$$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

$$m_N = 1 \text{ TeV}$$

$$a: B(\mu \rightarrow eee) = 10^{-12} \text{ for } m_N = 1 \text{ TeV}$$

$$\text{model 2: } a = b = c$$

$B(\mu \rightarrow e\gamma)$ : cancelation of  $N$ ,  $\tilde{N}$  and  $SB$  contributions

$$R_{\mu e}^{Au}, R_{\mu e}^{Ti} > B(\mu \rightarrow e\gamma)$$

$$R_1 \equiv \frac{B(l \rightarrow l' l_1 l_1^c)}{B(l \rightarrow l' \gamma)} \rightarrow \frac{\alpha}{3\pi} \left( \ln \frac{m_l^2}{m_{l'}^2} - 3 \right)$$

$$R_2 \equiv \frac{B(l \rightarrow l' l' l'^c)}{B(l \rightarrow l' \gamma)} \rightarrow \frac{\alpha}{3\pi} \left( \ln \frac{m_l^2}{m_{l'}^2} - \frac{11}{4} \right)$$

$$R_3 \equiv \frac{R_{\mu e}^J}{B(\mu \rightarrow e \gamma)}$$

$$\rightarrow 16\alpha^4 \frac{\Gamma_\mu}{\Gamma_{\text{capture}}} Z Z_{eff}^4 |F(-\mu^2)|^2$$

$(G_\gamma^L)_{l'l}, (G_\gamma^R)_{l'l}$  only:

$$R_1(\tau \rightarrow e \mu \mu) = 1/90,$$

$$R_1(\tau \rightarrow e \mu \mu) = 1/419$$

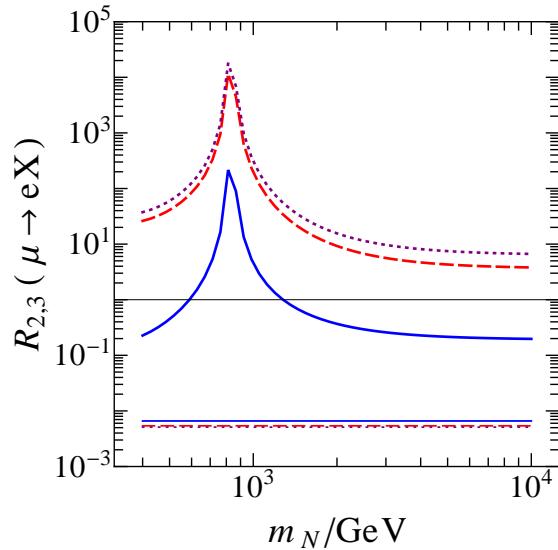
$$R_2(\mu \rightarrow e e e) = 1/159,$$

$$R_2(\tau \rightarrow e e e) = 1/91,$$

$$R_2(\tau \rightarrow \mu \mu \mu) = 1/460$$

$$R_3^{Ti} = 1/198,$$

$$R_3^{Au} = 1/188$$



$R_2(\mu \rightarrow e e e), R_3^{Ti}, R_3^{Au}$

$$m_0 = M_{1/2} = 1 \text{ TeV}, A_0 = -3 \text{ TeV}$$

$$m_N = 400 \text{ GeV}, \tan \beta = 10$$

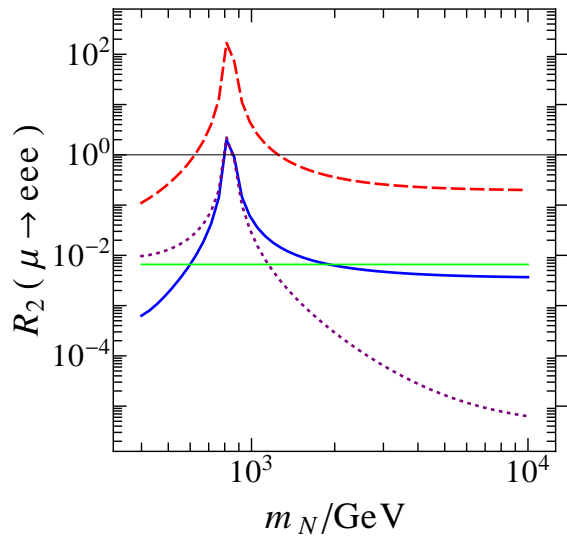
model 1 :  $a = b, c = 0$

$$R_2(\mu \rightarrow e e e): \text{full: } 0.2 - 10^2, (G_\gamma^{L,R})_{l'l} \text{ only: } 1/159$$

$$R_3^{Ti}: \text{full: } 3 - 10^4, (G_\gamma^{L,R})_{l'l} \text{ only: } 1/198$$

$$R_3^{Au}: \text{full: } 6 - 2 \times 10^2, (G_\gamma^{L,R})_{l'l} \text{ only: } 1/188$$

- source of strong enhancement?

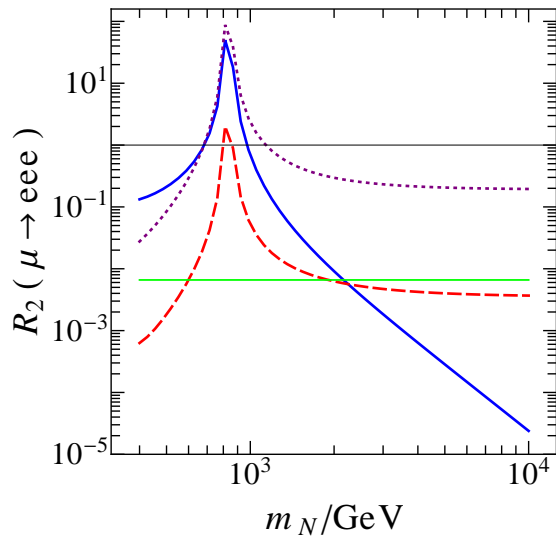


$R_2(\mu \rightarrow eee)$  : form factor contributions  
 $G_\gamma$  and  $F_\gamma$ ,  $F_Z$ , box,  $G_\gamma^{L,R}$  only

$\tan \beta = 10$

$a : B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV

- dominance of the  $F_Z$  contribution



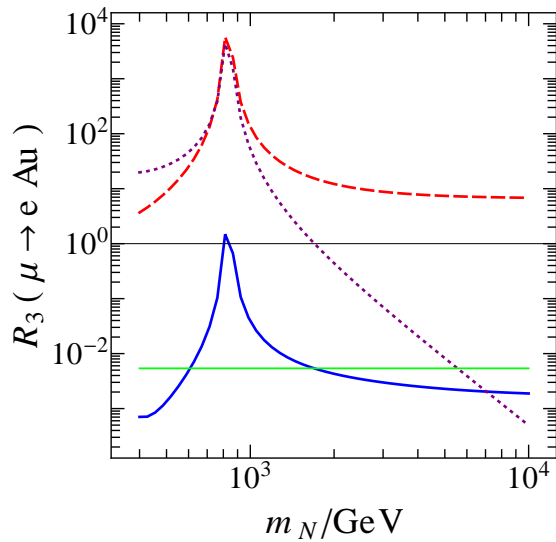
$R_2(\mu \rightarrow eee)$ :  $N$ ,  $\tilde{N}$ ,  $SB$ ,  $G_\gamma^{L,R}$  only

$\tan \beta = 10$

$a : B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV

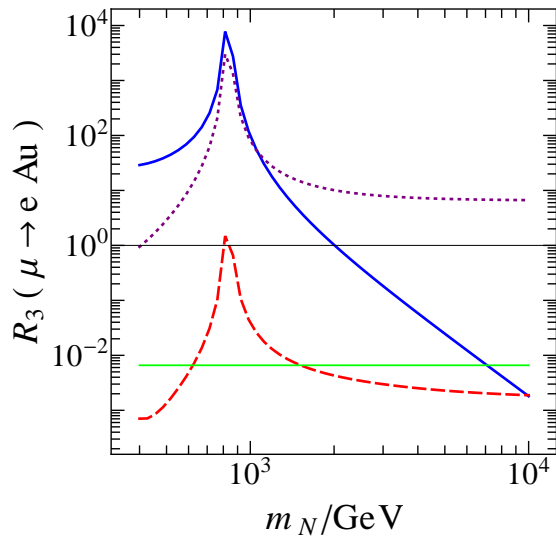
- dominance of  $N$  for  $m_N < 1$  TeV,

- dominance of  $SB$  for  $m_N > 1$  TeV



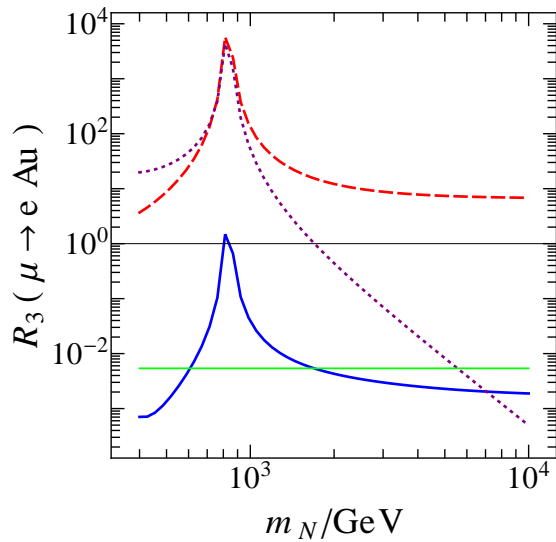
$R_3^{Au}$  : form factor contributions  
 $G_\gamma$  and  $F_\gamma$ ,  $F_Z$ ,  $\text{box}$ ,  $G_\gamma^{L,R}$  only  
 $\tan \beta = 10$

$a$  :  $B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV  
 - dominance of  $F_Z$  cont. for  $m_N > 1$  TeV  
 - dominance of  $\text{box}$  cont. for  $m_N < 1$  TeV



$R_3^{Au}$  :  $N$ ,  $\tilde{N}$ ,  $SB$ ,  $G_\gamma^{L,R}$  only  
 $\tan \beta = 10$

$a$  :  $B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV  
 - dominance of  $N$  cont. for  $m_N < 1$  TeV,  
 - dominance of  $SB$  cont. for  $m_N > 1$  TeV



$R_3^{Au}$  : form factor contributions

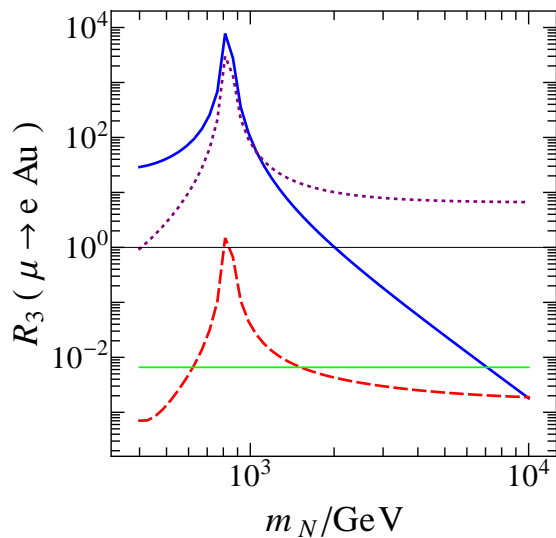
$G_\gamma$  and  $F_\gamma$ ,  $F_Z$ ,  $\text{box}$ ,  $G_\gamma^{L,R}$  only

$\tan \beta = 10$

$a : B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV

- dominance of  $F_Z$  cont. for  $m_N > 1$  TeV

- dominance of  $\text{box}$  cont. for  $m_N < 1$  TeV



$R_3^{Au}$ :  $N$ ,  $\tilde{N}$ ,  $SB$ ,  $G_\gamma^{L,R}$  only

$\tan \beta = 10$

$a : B(\mu \rightarrow e\gamma) = 10^{12}$  for  $m_N = 400$  GeV

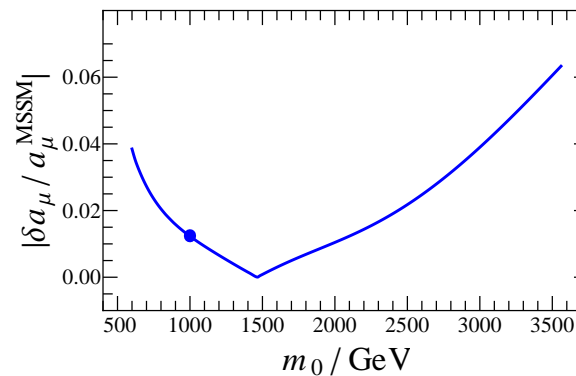
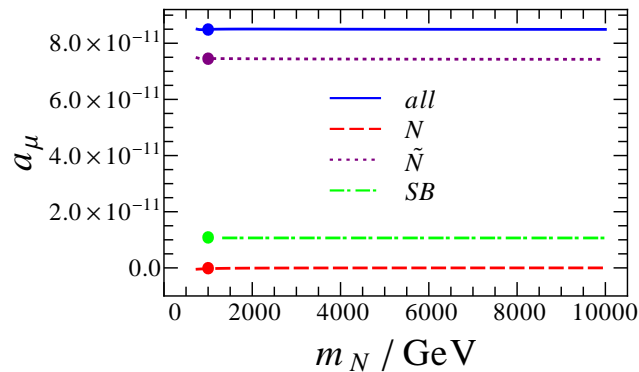
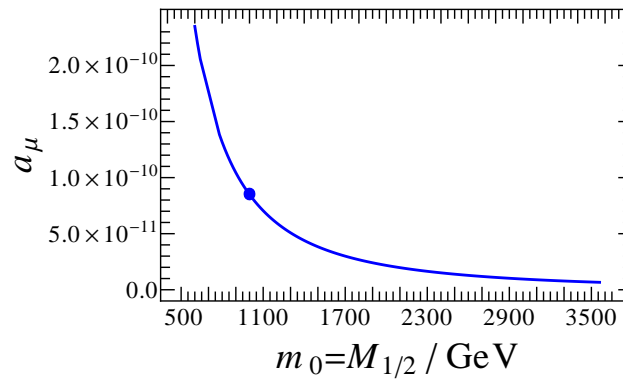
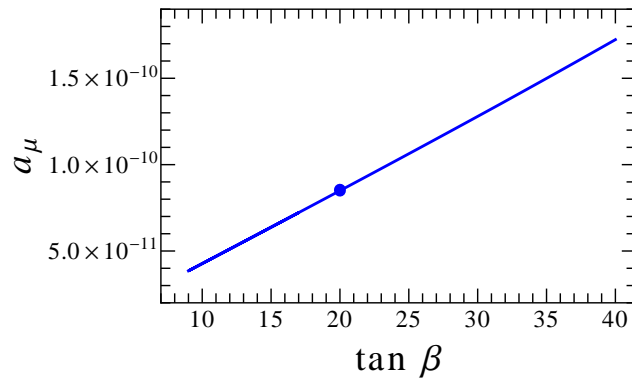
- dominance of  $N$  cont. for  $m_N < 1$  TeV,

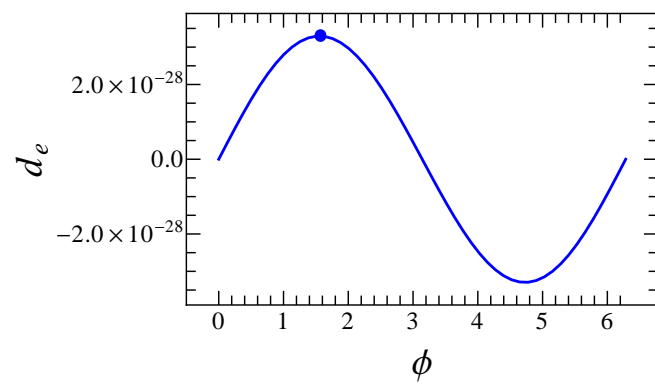
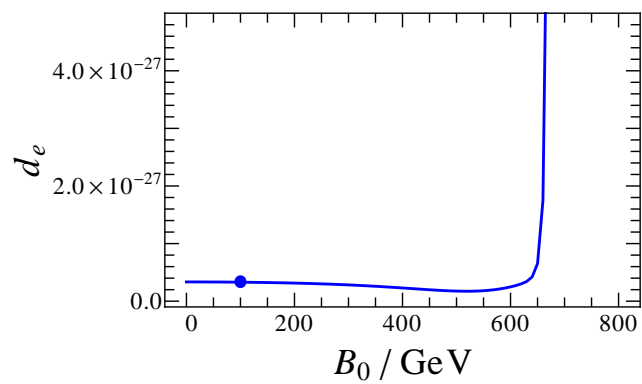
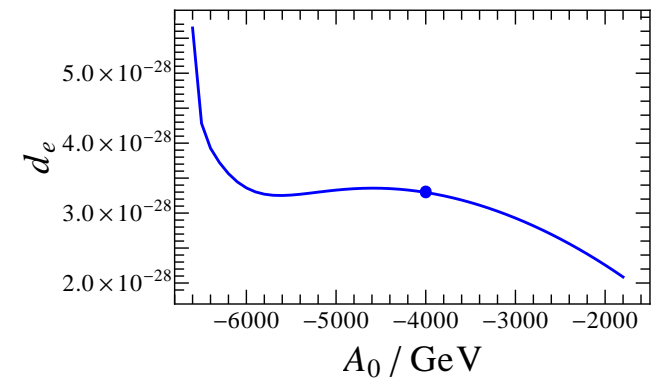
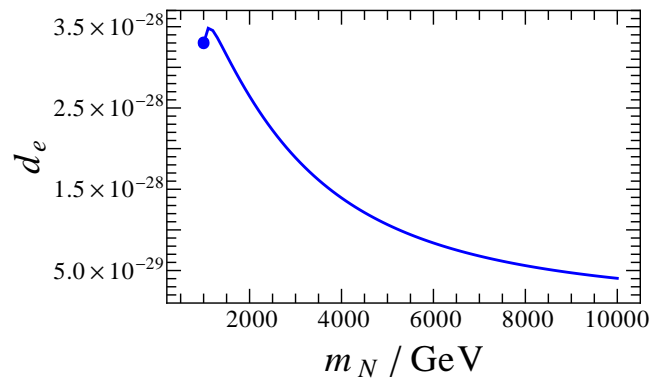
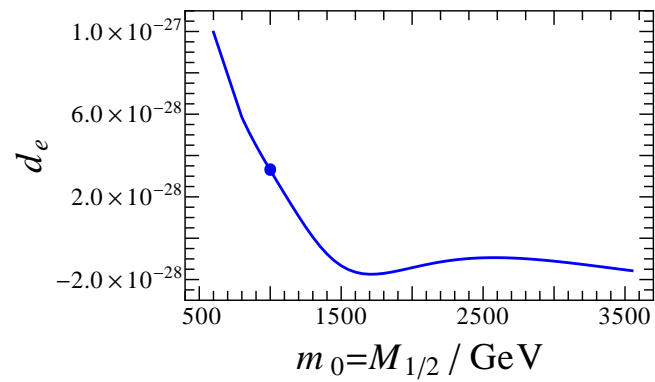
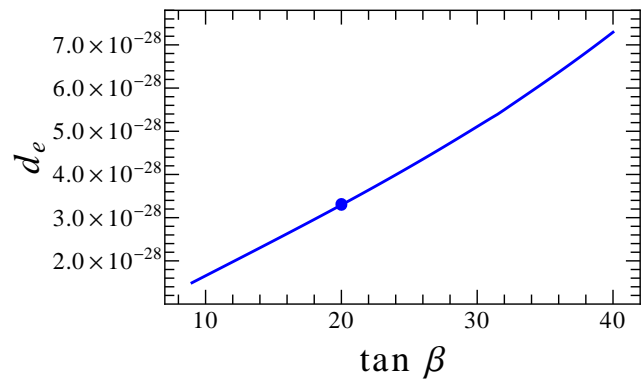
- dominance of  $SB$  cont. for  $m_N > 1$  TeV

# Numerical results for lepton dipole moments

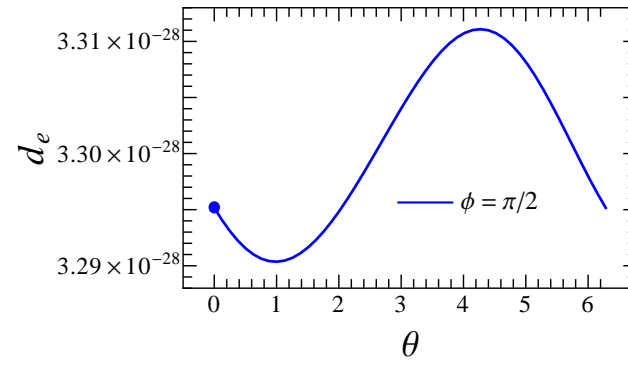
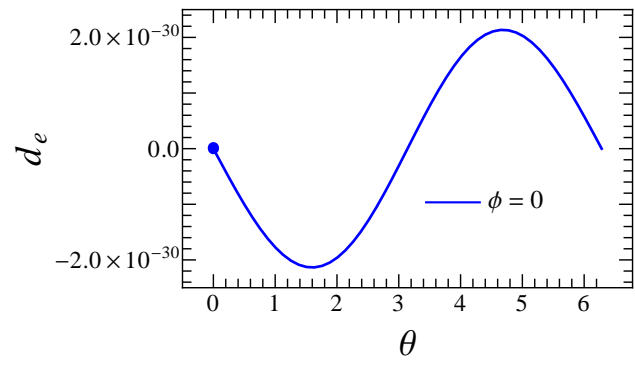
## Choice of baseline parameters

$$\begin{aligned}
 m_0 &= 1 \text{ TeV}, & M_{1/2} &= 1 \text{ TeV}, & A_0 &= -4 \text{ TeV}, & \tan \beta &= 20, \\
 m_N &= 1 \text{ TeV}, & B_0 &= 0.1 \text{ TeV}, & a &= b &= c &= 0.05,
 \end{aligned}$$









# Summary

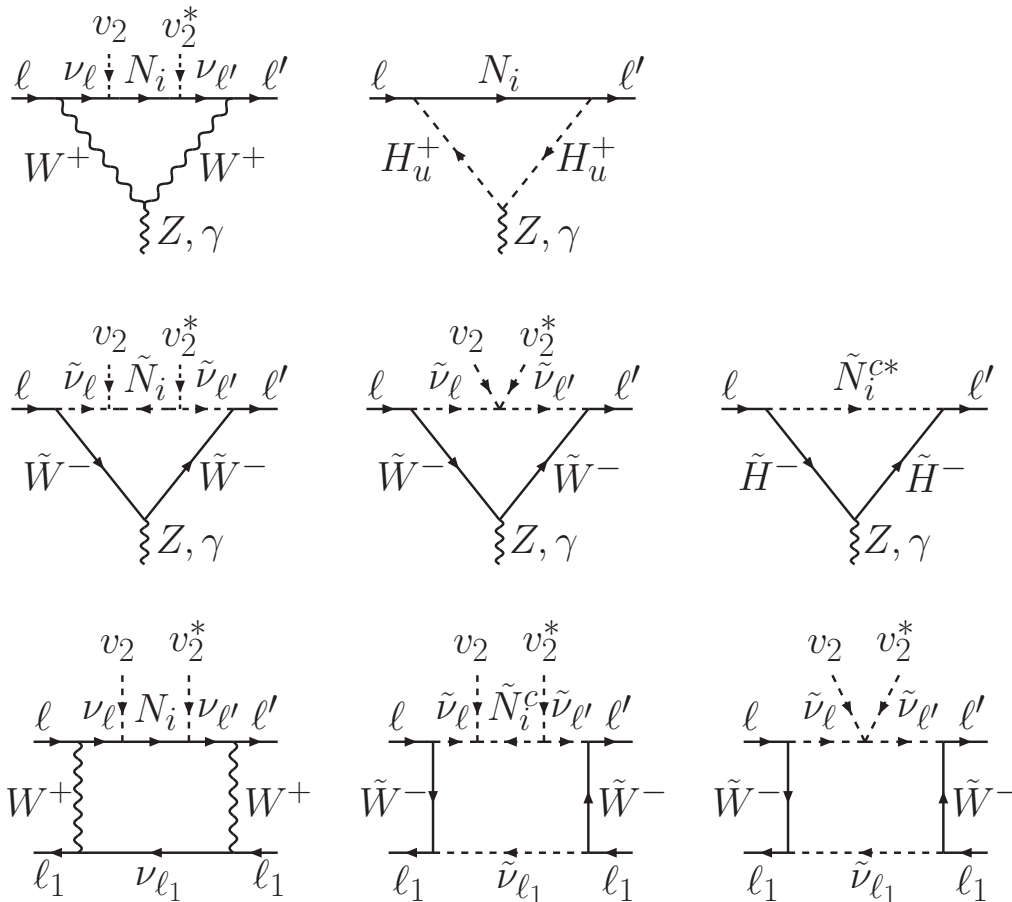
- We have carefully studied the  $N$ ,  $\tilde{N}$  and soft SB contributions to LFV. For the first time complete set of box diagrams is included. Complete set of chiral amplitudes is included  $(B_{\ell S}^{LR}, B_{\ell S}^{RL})$  - this decomposition is valid for any model.
- We have shown that in  $\mu \rightarrow eee$   $N$   $Z$ -boson-mediated graphs dominate for  $m_N < 1$  TeV and soft SB  $Z$ -boson-mediated graphs dominate for  $m_N > 1$  TeV. In  $\mu \rightarrow e$  conversion in nuclei  $N$  box graphs dominate for  $m_N < 1$  TeV and soft SB  $Z$ -boson-mediated graphs dominate for  $m_N > 1$  TeV. It is interesting that the low-scale seesaw model setup strongly influences soft SB part of the amplitude.
- Due to partial cancelation of  $N$  and  $\tilde{N}$  contributions in magnetic dipole amplitudes the  $l \rightarrow l'\gamma$  amplitudes are suppressed relative to other CLFV amplitudes.
- Due to perturbativity condition on Yukawa couplings, the CLFV amplitudes are dominated by quadratic Yukawa contributions, while quartic contributions are small.

- The dependence of LFV amplitudes on  $\tan\beta$  for  $5 \leq \tan\beta \leq 20$  is weak, except for  $l \rightarrow l'\gamma$  processes. ( $B_s \rightarrow \mu\mu$ )
- Relative to the MSSM with ordinary seesaw mechanism,  $l \rightarrow l'l_1l_2$  and  $\mu \rightarrow e$  conversion branching ratios are enhanced 2 – 3 orders of magnitude in the region of parametric space where are no accidental cancelations of amplitudes. Opposed to the high-scale seesaw MSSM models, in the low-scale seesaw MSSM models  $l \rightarrow l'l_1l_2$  and  $\mu \rightarrow e$  may give stronger constraint to the model parameters than  $l \rightarrow l'\gamma$  processes.
- We made an analysis of the lepton dipole moments, with particular regard to muon magnetic dipole moment  $a_\mu$  and electron electric dipole moment  $d_e$ . Up to our knowledge such analysis has been done for the first time in a model with a low scale seesaw mechanism. We showed that  $a_\mu$  satisfies scaling behaviour as in MSSM, and the heavy neutrino and sneutrino contributions do not numerically change the MSSM prediction for  $a_\mu$ . For  $d_e$  we found a scaling behaviour which almost agrees with the naive scaling prediction. That is new result. Further, at one loop level, only the additional phases of the soft SUSY breaking bilinear and trilinear couplings induce  $d_e$ , while the potential source of CPV from  $\nu_R$  MSSM vertices which are not complex conjugate to each other give numerically zero contribution to  $d_e$ . That is in accord with the result obtained for the one loop result for  $d_e$  in models with high scale seesaw mechanism.

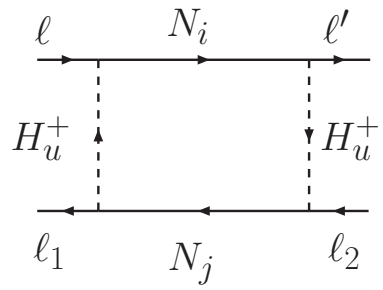
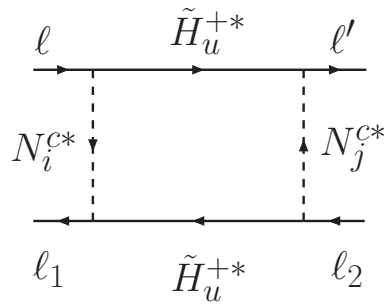
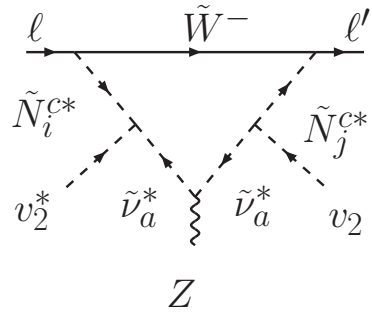
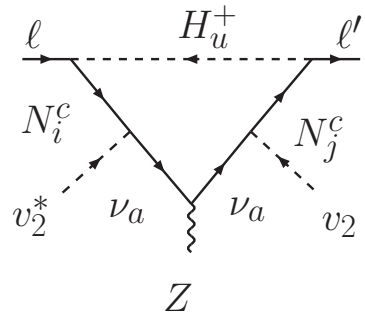
# Amplitudes : Dominant contributions

- dominant terms in lowest order in  $g_W$  and  $v_u$  ( $Y_\nu$ )

## Two Yukawas



# — Four Yukawas



## Form factors

$$(F_\gamma^{\ell\ell'})^N = \frac{\Omega_{\ell\ell'}}{6s_\beta^2} \ln \underbrace{\frac{m_N^2}{M_W^2}}_{=\lambda_N},$$

$$(F_\gamma^{\ell\ell'})^{\tilde{N}} = \frac{\Omega_{\ell\ell'}}{3s_\beta^2} \sum_{k=1}^2 \nu_{k1}^2 \ln \frac{m_N^2}{\tilde{m}_{\tilde{\chi}_k}^2},$$

$$(G_\gamma^{\ell\ell'})^N = -\Omega_{\ell\ell'} \left( \frac{1}{6s_\beta^2} + \frac{5}{6} \right)$$

$$(G_\gamma^{\ell\ell'})^{\tilde{N}} = \Omega_{\ell\ell'} \left( \frac{1}{6s_\beta^2} + g_\gamma \right)$$

$$g_\gamma = - \sum_{k=1}^2 \left[ \nu_{k1}^2 \frac{2M_W^2}{m_{\tilde{\chi}_i}^2} g_{\gamma,1} \left( \frac{m_{\tilde{\nu}}^2}{m_{\tilde{\chi}_i}^2} \right) + \nu_{k1} \mathcal{U}_{k1} \frac{\sqrt{2} M_W^2}{c_\beta m_{\tilde{\chi}_i}^2} g_{\gamma,2} \left( \frac{m_{\tilde{\nu}}^2}{m_{\tilde{\chi}_i}^2} \right) \right]$$

$$(F_Z^{\ell\ell'})^N = -\frac{3\Omega_{\ell\ell'}}{2} \ln \frac{m_N^2}{M_W^2} - \frac{\Omega_{\ell\ell'}^2}{2s_\beta^2} \frac{m_N^2}{M_W^2},$$

$$(F_Z^{\ell\ell'})^{\tilde{N}} = \frac{\Omega_{\ell\ell'}}{2} \ln \frac{m_N^2}{\tilde{m}_1^2} \left( -\frac{1}{2} + 2s_W^2 + \frac{1}{s_\beta^2} f_Z \right)$$

$$f_Z = \sum_{k,l=1}^2 \frac{m_{\tilde{\chi}_k} m_{\tilde{\chi}_l}}{M_W^2} (\mathcal{V}_{k2} \mathcal{U}_{k1} \mathcal{U}_{l1} \mathcal{V}_{l2} + \frac{1}{2} \mathcal{V}_{k2} \mathcal{U}_{k2} \mathcal{U}_{l2} \mathcal{V}_{l2} - s_W^2 \delta_{kl} \mathcal{V}_{k2} \mathcal{V}_{l2})$$

$$(F_{box}^{\ell\ell'l_1l_2})^N = -(\Omega_{\ell\ell'} \delta_{l_2l_1} + \Omega_{\ell l_1} \delta_{l_2l'}) + \frac{1}{4s_\beta^4} (\Omega_{\ell\ell'} \Omega_{l_2l_1} + \Omega_{\ell l_1} \Omega_{l_2l'}) \frac{m_N^2}{M_W^2}$$

$$(F_{box}^{\ell\ell'l_1l_2})^{\tilde{N}} = (\Omega_{\ell\ell'} \delta_{l_2l_1} + \Omega_{\ell l_1} \delta_{l_2l'}) f_{box}^\ell + \frac{1}{4s_\beta^4} (\Omega_{\ell\ell'} \Omega_{l_2l_1} + \Omega_{\ell l_1} \Omega_{l_2l'}) \frac{m_N^2}{M_W^2}$$

$$f_{box}^\ell = \sum_{k,l=1}^2 \mathcal{V}_{k1}^2 \mathcal{V}_{l1}^2 f_{box,1}^\ell(\lambda_{\tilde{\chi}_k}, \lambda_{\tilde{\chi}_l}, \lambda_{\tilde{\nu}}, \lambda_N) + \mathcal{V}_{k2} \mathcal{V}_{k1} \mathcal{V}_{l2} \mathcal{V}_{l1} f_{box,2}^\ell()$$

$$(F_{box}^{\ell\ell'uu})^N = -4(F_{box}^{\ell\ell'dd})^N = 4\Omega_{e\mu}$$

$$(F_{box}^{\ell\ell'uu})^{\tilde{N}} = \sum_{k,l=1}^2 \mathcal{V}_{k1}^2 \mathcal{V}_{l1}^2 f_{box}^u(\lambda_{\tilde{\chi}_k}, \lambda_{\tilde{\chi}_l}, \lambda_{\tilde{d}}, \lambda_N)$$

$$(F_{box}^{\ell\ell'dd})^{\tilde{N}} = \sum_{k,l=1}^2 \mathcal{V}_{k1}^2 \mathcal{V}_{l1}^2 f_{box}^d(\lambda_{\tilde{\chi}_k}, \lambda_{\tilde{\chi}_l}, \lambda_{\tilde{u}}, \lambda_N)$$

## SUSY limit; cancelations, enhancements:

-  $\tilde{m}_{\tilde{\chi}_{1,2}}^2 \xrightarrow{SL} M_W^2$ ,  $t_\beta \xrightarrow{SL} 1$ ,  $\mu \xrightarrow{SL} 0$  (Barbieri, Giudice PLB309)

-  $(G_\gamma^{\ell\ell'})^N + (G_\gamma^{\ell\ell'})^{\tilde{N}} \stackrel{SL}{=} 0$ : Ferrara, Remiddi PLB53 (1974) 347

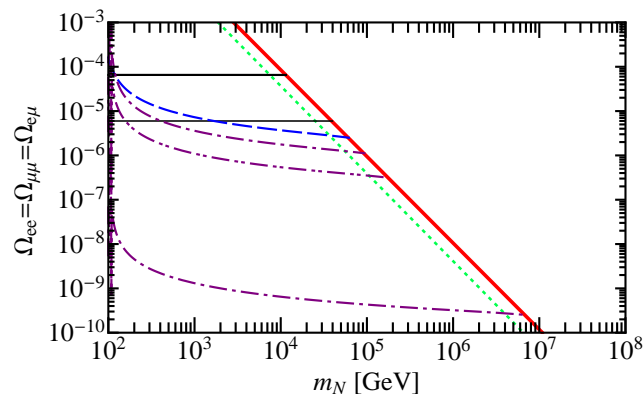
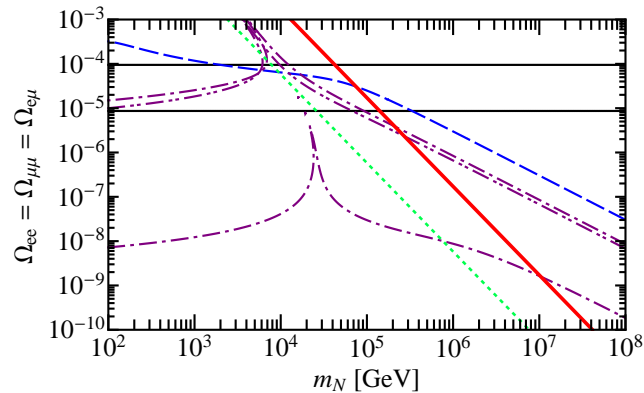
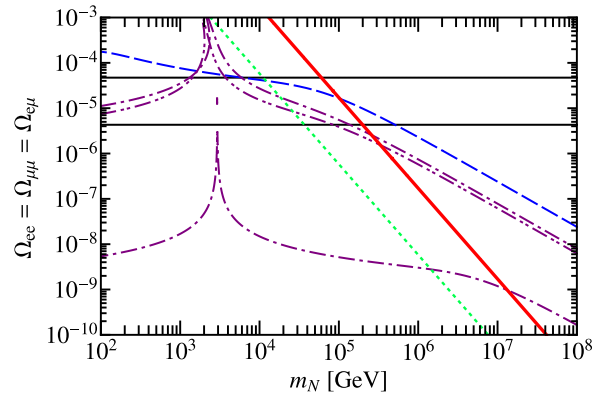
- box form factors : positive interference

-  $Y_\nu^4$  terms : become important when  $Y_\nu/g_W \sim 1$   $(\Omega_{\ell\ell'} \frac{m_N^2}{M_W^2} = 2(Y^\dagger Y)_{\ell\ell'} / g_W^2)$

(A. Pilaftsis, A.I, NPB437 (1995) 491)



# Numerical estimates



$$\tan \beta = 3$$

$$m_0 = 100 \text{ GeV}, M_0 = 250 \text{ GeV}$$

$$A_0 = 100 \text{ GeV}$$

$$\Omega_{\mu e} = \Omega_{ee} = \Omega_{\mu\mu}, \text{ other } \Omega_{\ell\ell'} = 0$$

## Upper bounds

$$B(\mu^- \rightarrow e^- \gamma) \quad 1.2 \times 10^{-11} \quad [1]$$

$$1 \times 10^{-13} \quad [2]$$

$$B(\mu^- \rightarrow e^- e^- e^+) \quad 1 \times 10^{-12} \quad [1]$$

$$R_{\mu e}^{Ti} \quad 4.3 \times 10^{-12} \quad [3]$$

$$1 \times 10^{-18} \quad [4]$$

$$R_{\mu e}^{Au} \quad 7 \times 10^{-13} \quad [5]$$

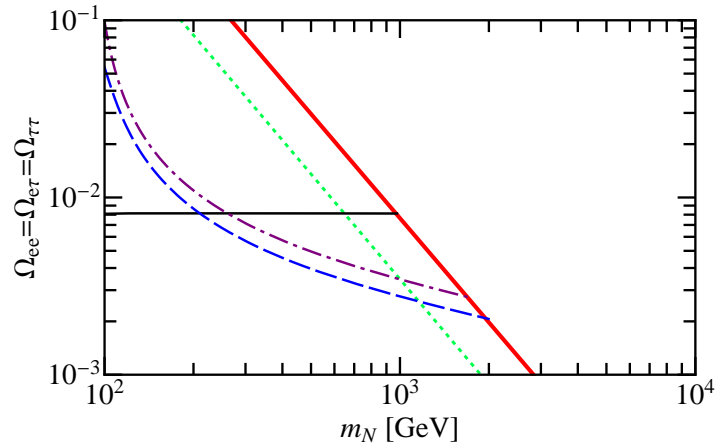
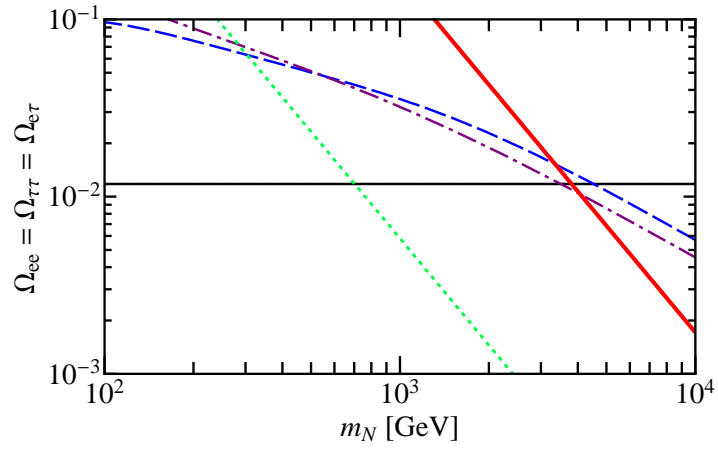
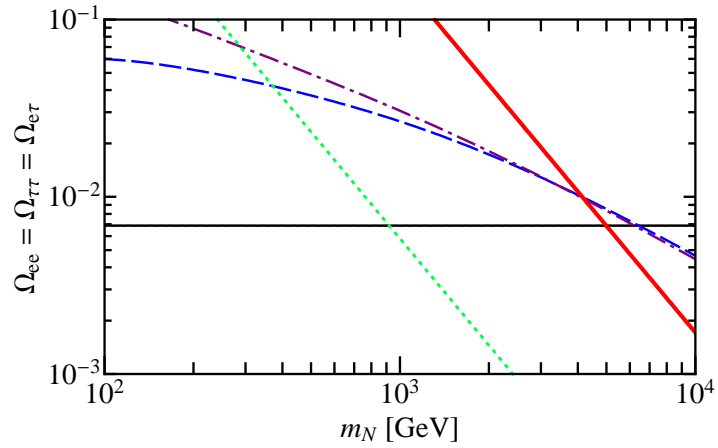
[1] Amsler, PLB 667 (2008) 1

[2] Ritt, NPBPS 162 (2006) 279

[3] Dohmen, PLB 317 (1993) 631

[4] Kuno, NPBPS 149 (2005) 376

[5] Bertl, EPJC 47 (2006) 337



$$\Omega_{\tau e} = \Omega_{ee} = \Omega_{\tau\tau}, \text{ other } \Omega_{\ell\ell'} = 0$$

### Upper bounds

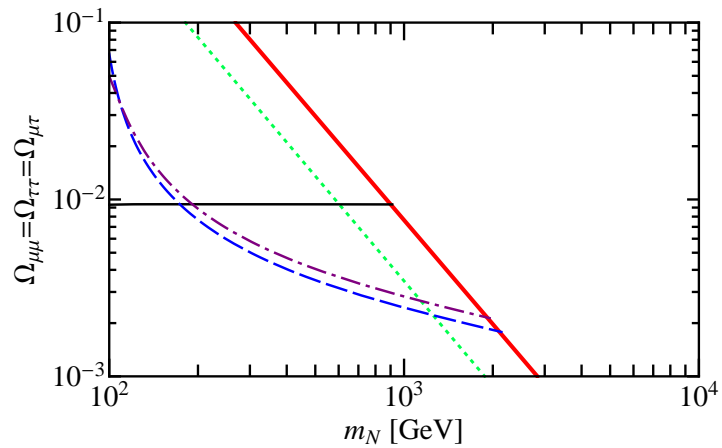
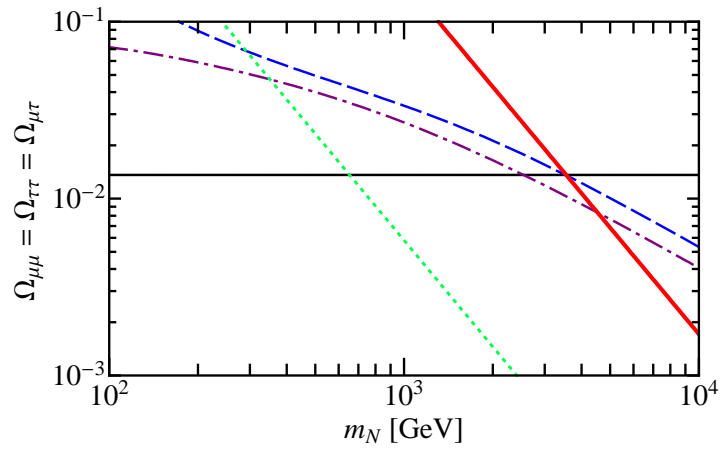
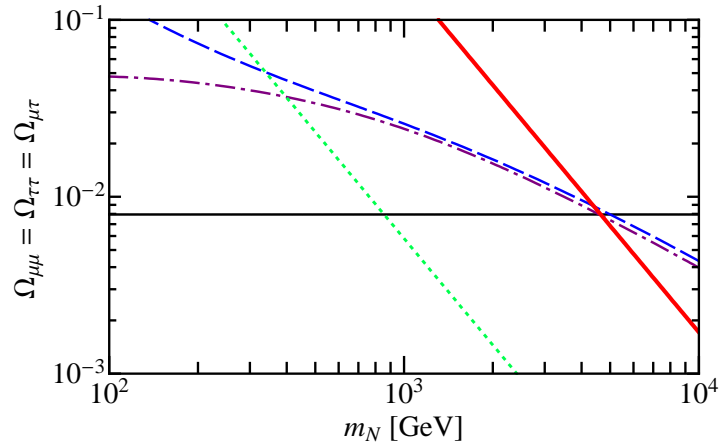
$$B(\tau^- \rightarrow e^- \gamma) \quad 3.3 \times 10^{-8} \quad [1]$$

$$B(\tau^- \rightarrow e^- e^- e^+) \quad 2.7 \times 10^{-8} \quad [2]$$

$$B(\tau^- \rightarrow e^- \mu^- \mu^+) \quad 2.7 \times 10^{-8} \quad [2]$$

[1] Aubert, PRL 104 (2010) 021802

[2] Hayasaka, PRL 687 (2010) 139



$$\Omega_{\tau\mu} = \Omega_{\mu\mu} = \Omega_{\tau\tau}, \text{ other } \Omega_{\ell\ell'} = 0$$

### Upper bounds

$$B(\tau^- \rightarrow \mu^- \gamma) \quad 4.4 \times 10^{-8} \quad [1]$$

$$B(\tau^- \rightarrow \mu^- \mu^- \mu^+) \quad 2.1 \times 10^{-8} \quad [2]$$

$$B(\tau^- \rightarrow \mu^- e^- e^+) \quad 1.8 \times 10^{-8} \quad [2]$$

[1] Aubert, PRL 104 (2010) 021802

[2] Hayasaka, PRL 687 (2010) 139

# Summary

- We have shown that in the low-scaled supersymmetric seesaw models sneutrinos might give large effects independent of SUSY breaking mechanism.
- Due to SUSY the  $\ell \rightarrow \ell' \gamma$  are suppressed.
- That makes  $\mu \rightarrow e$  conversion especially interesting candidate for finding LFV.  $\mu \rightarrow 3e$  and  $\tau \rightarrow 3e$  give complementary information on LFV.
- Inclusion of the mSUGRA boundary conditions strongly influences the final results of the model. Particularly it leads to a larger theoretical prediction for LFV observables  $R_{\mu e}$ ,  $\mu \rightarrow 3e$  and  $\tau \rightarrow 3e$  by up to a factor of 25. The branching fractions for  $\ell \rightarrow \ell' \gamma$  variation show smaller variation – they are slightly larger than those obtained in MSSM+3N without mSUGRA boundary condition, but larger than results obtained in non-supersymmetric version of the model.